# ICMERE2015-PI-113

## ENHANCEMENT OF HEAT TRANSFER USING U-SHAPED TWISTED TAPE INSERTS IN DIFFERENT SPACING FOR TURBULENT FLOW

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Abstract: This work was experimented the turbulent flow heat transfer in a tube having different spacings U shaped twisted tape inserts in U-shape with water as working fluid. The test section consisted of a circular copper tube of 26.6 mm inner diameter, 900 mm length with five K-type thermocouples. Bulk temperature and pressure drops were measured. The aluminum inserts were 800 mm in length, 25 mm width, 1.5 mm thickness and twisted ratio of 5 was used. Heat flux, friction factor and Nusselt number were calculated to analysis heat transfer performance of circular tube fitted with/without inserts in turbulent regimes (4000 < Re < 20000). Heat transfer rate for inserts 25 mm, 40 mm and 80 mm in spacings in U-shapewas increased by 4, 3, 2 and Nusselt number was risen by1.2, 1.18, 1.06 times respectively compared to smooth tube. Heat transfer performance for inserts were found 1.57~1.67, 1.32~1.40, 1.17~1.27 times better than smooth tube and selected 25 mm spacings as the best compared to others.

Keywords: U-shape insert, Heat transfer rate, Friction factor, Pressure drop, Heat transfer performance.

### 1. INTRODUCTION

Heat transfer augmentation technique is improving continuously. The study to increase heat transfer has been started at the beginning of twentieth century. Many investigations are already successfully completed and being used in many sectors. According to the modern studies, it is observed that the performance dealt with 'U-shape twisted tape inserts 'is the most economical heat transfer enhancement tool. It is important to verify the implementation of heat exchanger tool to know the tube side as well as shell side heat transfer. Heat exchanger is the tool which provides heat transfer between two or more fluids and develops the high performance thermal system. It improves the heat exchanger effectiveness for internal and external flows. Naturally, the mixing of the fluids are increased by increasing flow vorticity, unsteadiness, turbulence or by limiting the growth of fluid boundary layers close to the heat transfer surfaces.

Heat transfer augmentation techniques are widely used in areas specified as temperature effort transform, air conditioning and preservation systems and chemical reactors. Basically the experiments are studied, using different shapes of inserts, different types of materials, in varieties experimental works for dissimilar environments. Due to rapid growth of industrialization the research on this topic has been enlarged significantly. Nowadays it is one of the most important topics to enhance heat transfer with minimizing the material cost. Many researches have been carried out to increase convective heat transfer for various flow conditions, reducing friction factor and use of power. Bergles et al. [1] declared the obtainable literature on convection temperature soul. According to the literature, the augmentation techniques were classified into two categories (Passive and active). Passive augmentation techniques, which required no external power, and active techniques, which do required external power. The fourteen techniques were grouped in terms of their application to the various modes of heat transfer. Mass transfer was included for completeness. The nonviolent methods were supported on the identical principle. Use of this technique causes the whirl in the volume of the fluids and disturbs the literal line layer so as to growth strong articulator mass devices were generally victimized as supine alter transpose enhancement techniques:

- Inserts
- Extended aboveground
- Shallow modifications
- Use of additives.

U-shape twisted tap insert provides an additional disturbance to the fluid in the section of the tube wall and vorticity behind the cuts and thus leads to a higher energy soul improvement in comparison with smooth tube. Salam et *al.* [2] made an investigation to enhance tube side heat transfer with rectangular shaped twisted tape insert. It was observed that, the Reynolds numbers were varied from

10000 to 19000 ranges with heat flux variation rangingfrom14 to 22 kW/m<sup>2</sup> for smooth tube and 23 to 40 kW/m<sup>2</sup> for tube with insert. Nusselt numbers for smooth tube were compared with Gnielinski correlation and errors were found from -6% to -25% ranges with R.M.S. value of 20%.Nusselt numbers in tube with rectangular-cut twisted tape insert were enhanced by 2.3 to 2.9 times with the increase of friction factors by 1.4 to 1.8 times compared to the smooth tube. Heat transfer enhancement efficiencies were found in the range of 1.9 to 2.3 and increased with the increase of Reynolds number. Mesh or spiral brush inserts were used by Megerlin et al. [3] to enhance heat transfer in short channels subjected to high heat flux. For turbulent flows the heat transfer coefficient can be developed as much as 8.5 times that in a smooth tube, but pressure drop was very high. Sarada et al. [4] made an investigation with varying width twisted tape inserts ranging from 10 mm to 26 mm. The Reynolds number varied from 6000 to 13500. It was found that the increment of heat transfer with twisted tape inserts as compared to plain tube varied from 36~48% for width 26 mm and 33~39% for width 22 mm inserts. A new idea was postulated by Hsieh and Huang [5] to foretell heat transfer and pressure drop of laminar flow in horizontal tubes with/without longitudinal inserts. They said that enhancement of heat transfer as compared to a conventional bare tube at the same Reynolds number to be a factor of 16 at Re  $\leq$  4000, while a friction factor rise of 4.5.Friction and heat transfer characteristics of turbulent air flowing through tubes with twisted strip swirl promoters were studied experimentally and analytically by Thorsen and Landis [6]. Data were obtained for pitch-to-diameter ratios as low as 3.15 and for Reynolds numbers up to 100,000. Both heating and cooling tests were run for tube wall to fluid bulk temperature ratios from 0.6 to 1.9 to assess compressibility and buoyancy effects. Eiamsa-ardet al.[7] conducted an experimental study for a round tube with short-length twisted tape insert on the mean Nusselt numbers, friction factor and enhancement efficiency characteristics under uniform wall heat flux boundary conditions. For swirling flow, the short-length tape was established for generating a strong swirl flow at the tube entry when the full-length twisted tape was inserted into the tube at a single twist ratio of y/w=4.0. The enhancement efficiency with the short-length insert was found to be lower than that with the full-length insert. Eiamsa-ardet al.[8] were continued the investigations and used DI-coil in common with the insert at lower Reynolds number and found the highest thermal performance factor of around 1.25. Again, Eiamsa-ardet al.[9] made an experiment using single twisted tapes and full-length dual twisted tapes with three different twist ratios (y/w=3.0, 4.0 and 5.0) and also regularly-spaced dual twisted tapes with three different space ratios (s/D=0.75, 1.5 and 2.25). The result observed that the heat transfer of the tube with dual twisted tapes was higher than that of the plain tube with/without single twisted tape insert. Altaie et al.[10] studied with ribs assembly of 5x5 mm cross section and fitted in the tube and separated by 8cm pitch. Results of temperature and velocity distribution along the tube center line for the case of tube with internal ribs were compared with that of plain tube, those results showed that the use of internal ribs enhance the heat transfer rate and found to possess the highest performance factors for turbulent flow. Heat transfer performance for turbulent flow in a circular tube with a porous/perforated twisted tape insert was experimentally investigated by Wazed et al. [11]. In the analysis a wide range of Reynolds numbers  $(1.3 \times 10^4 \text{ to } 5.2 \times 10^4)$  were observed. The heat transfer coefficient was enhanced (up to 5.5 times) in the cost of increasing pumping power (1.8 times) in turbulent flow through a tube with the inserts. The heat transfer effectiveness in a tube with a perforated twisted tape insert was found to increase up to 4.0 times compared with the value for the plain tube. An investigational research of heat transfer performance of porous twisted tape insert in a circular tube was carried out by Ahamed et *al.* [12]. In arrange of Reynolds number 1.3 x  $10^4$  to 5.2 x  $10^4$ the results found for tube with porous twisted tape insert, the average heat transfer coefficient was 2.60 times higher, the heat flux was 1.55 times higher, the friction factor was 2.25 times higher and the pumping power was 2.0 times higher than plain tube values.

U-shape twisted tape is very economic and also reduce the pressure drop as well as uses of material. The experiment focuses on convection heat transfer enhancement inside the tube by using U-shaped twisted tape inserts. The main aim of the current research was to find the heat flux and pressure drop using U-shaped twisted tape inserts of different U-shaped spacing's to choose the best one. Another important finding was to determine the efficiency of three different inserts and choose the best among them comparing with smooth tube.

There were some limitations according to the study. It was not easy to use twisted inserts in turbulent flow region as the value of pressure drop was high. So, high cost required to do this experiment. Lower twist ratio offered higher heat transfer rate than the higher twist ratio because intensity of turbulence and flow length obtained from lower twist ratio was high. It was hard to handle this process without heat loss. The heater could not wrap properly, therefore equal distance was not found in every curl. The bulk temperatures were measured by average of input and output temperatures.

## 2. METHOLDOLOGY

A good experimental system is necessary to get better and appropriate result which helps to accelerate the study of heat transfer augmentation. In the existing project, three Ucut twisted tape inserts of aluminum strips were used. The inserts length were 800 mm, width were 25 mm and

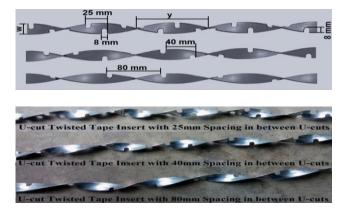


Fig.1: U-shape twisted tape inserts.

thickness were 1.5 mm. Twisted ratio of 5 and the width and depth of 8 mm of the U-shaped was used. The inserts varied in the U-shaped spacings and the spacing's were 25 mm, 40 mm and 80 mm respectively. Figure 1 displays the design of the inserts used in the current experiment.

A schematic diagram of the experimental setup is shown in fig 2. A long copper tube of 26.6 mm internal diameter and 30 mm outer diameter and length of 900 mm was used as the test section. A nichrome wire was wrapped around the test section in a periodic distance to heat the whole section equally. Therefore, constant heat flux condition was maintained. To avoid heat loss, sufficient quantity of fiber glass insulation was used with mica sheet wrapped over the wire. Outer surface temperature of the tube was measured at five points of the test section maintaining equal distance from one point to another point by K-type thermocouples. Two thermometers were used at the inlet and outlet section of the tube for evaluating the bulk temperature. Pressure drop was measured at inlet and outlet of the test section. A manometer was used to determine the pressure drop at inlet and outlet of the test section. Open loop system of water supply was used. From a continuous water system, the water was forced in the reservoir and then using a pump, water was pumped into the test section have shown in fig 2. A gate valve was placed in between the reservoir and the

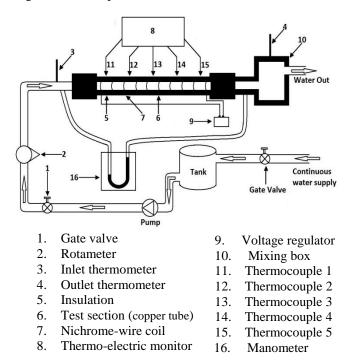


Fig.2: Schematic diagram of the experimental setup.

test section to control the flow of water. The rate of flow was measured with the support of rotameter(Metric 24G, SS float) of 26 L/min capacity in the travelling path of inlet water. Data were collected for smooth tube and using the inserts in smooth tube.

In the beginning, the tank was filled by water from a continuous source and then pumped to the test section through rotameter. The flow was controlled by a gate valve to make it steady. The flow rate of water was varied from a range of minimum 5.4 L/min and maximum 20.7 L/min measured by the rotameter. After switching on the heating

unit, enough time was given to achieve the steady state condition. Then using thermometers, the inlet and outlet temperature of water were taken. After that, data were collected from the K-type thermocouples. A menometric pressure drop was counted for a single flow rate by a manometer. In each run of water into the tube, data were taken for water flow rate, inlet temperature, outlet temperature, tube outer surface temperatures and pressure drop readings in the prospective way.

#### 3. MATHEMATICAL FORMULATIONS

Heat transfer performance of insert in water at circular tube was calculated by using the following equations.

Outer surface area was calculated from,  $A_0 = \pi d_0 L$  (3.1) Where,  $d_0$  is outer surface diameter.

Inner surface area was calculated from,  $A_s = \pi d_i L$  (3.2) Where,  $d_i$  is outer surface diameter.

| The experimental friction co-efficient, | $f = \frac{2\Delta P d_i}{\rho L u_m^2};$ | (3.3) |
|---|---|-------|
|---|---|-------|

Where, mean velocity, 
$$u_{\rm m} = \frac{{\rm m}}{{\rm A_f}}$$
, (3.4)

Flow area, 
$$A_f = \frac{\pi}{4} d_i^2$$
 (3.5)

Pressure difference was obtained from,  $\Delta p = \Delta h \times \rho \times g \times 13.6$ 

 $\Delta \mathbf{p} = \Delta \mathbf{h} \times \mathbf{\rho} \times \mathbf{g} \times 13.6 \tag{3.6}$ 

Added heat was calculated by,  $Q = mc_p(T_o - T_i)$  (3.7)

Velocity, 
$$V = \frac{m}{A_x}$$
; (3.8)  
Where m is flow rate and

Where, m is flow rate and

Cross sectional area, 
$$A_x = \frac{\pi d_i^2}{4}$$
 (3.9)

- Reynolds Number,  $Re_D = \frac{\rho V d_i}{\mu}$  (3.10)
- Nusselt number,  $Nu_{exp} = \frac{hd_i}{k}$  (3.11)

Dittus Boelter equation,

$$Nu_{D} = 0.023 Re_{D}^{5} Pr^{n};$$
(3.12)  
Where n is 0.4 for heating and 0.3 for cooling.

Prandtl number,  $\Pr = \frac{\mu c_p}{k}$ ; (3.13)  $\mu$  and k at bulk temperature.

Convective heat transfer coefficient was calculated from,

$$h = \frac{Q}{A(T_{wi} - T_b)}$$
(3.14)

And heat flux was found from, 
$$q = \frac{Q}{A_s}$$
 (3.15)

Theoretical friction factor was calculated from,  $f_i = (0.79 \ln Re - 1.64)^{-2}$  (3.16) Bulk temperature,  $T_b = \frac{T_i + T_o}{2}$  (3.17)

Outer surface temperature, 
$$T_{w0} = \sum_{i=1}^{5} \frac{T_{w0,i}}{5}$$
 (3.18)

Inner surface temperature,  $T_{wi} = T_{w0} - Q \frac{\ln(d_0 - d_i)}{2\pi k_w L}$  (3.19)

% of error = 
$$\left(\frac{Nu_{exp} - Nu_D}{Nu_D}\right)$$
 100 (3.20)

Efficiency, 
$$\Pi = \left(\frac{Nu_{exp}}{Nu_D}\right) / \left(\left(\frac{f}{f_i}\right)^{\frac{1}{3}}\right)$$
 (3.21)

All the fluid properties were evaluated at bulk temperature.

#### 4. RESULTS AND DISCUSSION

Initially, Nusselt numbers were calculated to compare the data with Dittus and Boelter[13] values found from Eq. (3.12) and errors were found within -3.82% and +6.5% ranges with R.M.S. error value of 4.75%. For smooth tube, using Eq. (3.10) the results were found that the Reynolds number values varied in 4949.14 to 18971.72 ranges, which were remain unchanged after using inserts.

Heat transfer rate was found from the Eq. (3.7) in the range of 376.11 to 1441.76 W for smooth tube without insert. Convective heat transfer coefficient was found in ranges of790.16 to 3057.83 W/m<sup>2</sup>.°c, Nusselt number was calculated from Eq. (3.11) and got the result in between 33.96 to 131.62ranges, and friction factor raised in range of 0.022 to 0.057 and heat transfer enhancement efficiency varied in0.94 to 1.26 ranges for plain tube.

Afterward, using the insert of 25 mm spacing between Ushapes the results were obtained that heat transfer rate was found in the range of 1504.44 to 5767.02 W, convective heat transfer coefficient in 956.50 to 3709.03 W/m<sup>2</sup>.°c ranges, Nusselt number in between 41.10 to 159.64 ranges, friction factor was promoted from 0.18 to 0.391 ranges found from Eq. (3.3), where pressure drop was measured by applying Eq. (3.6), and heat transfer enhancement efficiency was improved from 1.57 to 1.98 ranges.

Next, by using the insert of 40 mm spacing between Ushapes the results were obtained that heat transfer rate foundin 1128.33 to 4325.27 W ranges, convective heat transfer coefficient varied from 931.37 to 3610.45 W/m<sup>2</sup>.°c ranges, Nusselt number was found in the range of 40.02 to 155.40, friction factor values were obtained from 0.098 to 0.213 ranges, and heat transfer enhancement efficiency increased from 1.32 to 1.66 ranges was found by applying Eq. (3.21).

When, the insert of 80 mm spacing between U-shapes was used, the results found for heat transfer rate in 752.22 to 2883.51 W ranges, convective heat transfer coefficient varied from 834.83 to 3232.45 W/m<sup>2</sup>.°c ranges, Nusselt number in 35.87 to 139.13 ranges, friction factor values found in between 0.052 to 0.107 ranges and heat transfer enhancement efficiency raised in 1.19 to 1.47 ranges.

The variation of Nusselt number with Reynolds number for smooth tube and tube with U-shape twisted tape inserts are shown in fig 3. It was found that, Nusselt number

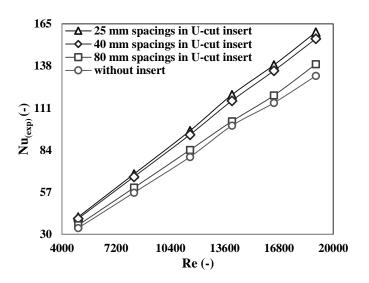


Fig.3: Variation of Nusselt number with Reynolds number.

increased with the increment of Reynolds number. The maximum value was found for inserts of 25 mm spacings in U-shape. Nusselt number increased with three inserts of 25 mm, 40 mm and 80 mm in spacing between U-shapes by 1.20,1.18, 1.06 times respectively compared with the smooth tube. The insert having 25 mm spacings in U-shape selected as the best insert among the others.

It was found that for the increasing of same Reynolds number, increased the heat transfer rate with three inserts of 25mm, 40 mm and 80 mm in spacing between U-shapes by 4.00, 3.00, 2.00 times respectively compared with the smooth tube. From fig 4 the heat transfer rate with the

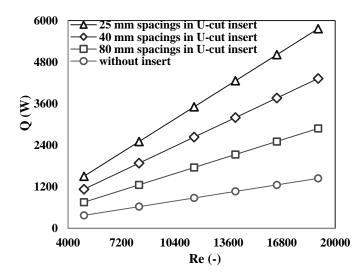


Fig.4: Variation of heat transfer rate with Reynolds number.

insert of 25 mm spacings was higher than that of the others. As insert was used, the heat transfer rate was increased and more disturbances in flow causes more heat transfer.

From fig 5 it was found that for increasing of Reynolds number decreased friction factor with three inserts of 25 mm,40 mm and 80 mm in spacing between U-shapes of 6.85to 8.18, 3.74 to 4.45, 1.88 to 2.36 times respectively while comparing with smooth tube. The friction factor with

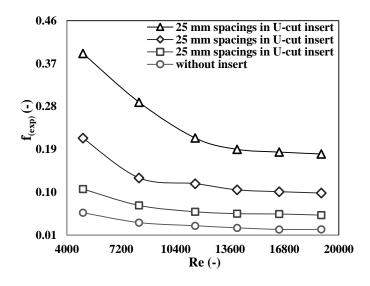


Fig.5: Variation of friction factor with Reynolds number.

insert of 25 mm spacings was discovered maximum. The cause was while inserts were being used, it increases pressure drop.

From fig6 it was found that for the continuous increasing of Reynolds number the heat transfer coefficient was detected 1.20, 1.18 and 1.06 times better respectively with three twisted tape inserts of 25 mm, 40 mm and 80 mm spacing in between U-shapes comparing with the

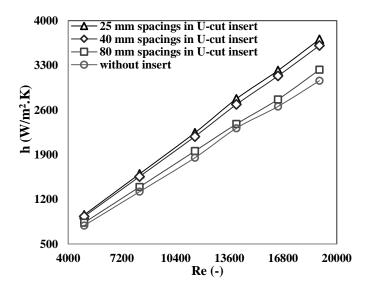


Fig.6: Variation of convective heat transfer coefficient with Reynolds number.

smooth tube. But the resulting value of insert with 25 mm spacing was maximized. Because, when insert was used heat transfer rate was increased, and thus for a smaller gape in between U-shapes, it increased rapidly.

From fig 7, it was found that for the increasing of same Reynolds number, heat transfer enhancement efficiency was increased. Comparing with the smooth tube the increment found in the range of 1.57~1.67, 1.32~1.40, 1.17~1.27 times for three inserts of 25 mm, 40 mm and 80 mm in spacing between U-shapes respectively. But the efficiency with insert of 25 mm spacing was higher than the others as it provided more eddy during the flow of fluid.

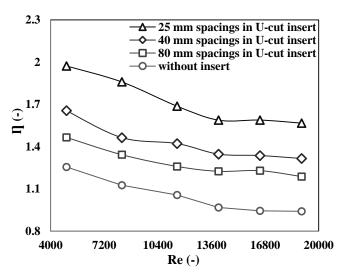


Fig.7: Variation of heat transfer enhancement efficiency with Reynolds number.

So that, when inserts were used efficiency was increased and among the used inserts, 25 mm spacings in U-shapes twisted tape insert was better.

#### 5. CONCLUSIONS

Experimental exploration of heat transfer, friction factor and heat transfer enhancement efficiency of a circular tube with U-shaped twisted tape inserts with different spacings of 25 mm, 40 mm and 80 mm are hit off in the current narration. The results can be drawn as follows:

- I. The Nusselt number and friction factor values for the tube with U-shape twisted tape inserts were noticeably higher than that of smooth tube and highest value found for 25 mm spacings in Ushapes insert. The values found 1.2 times better in Nusselt Number and 6.85 to 8.18 times improved in friction factor with respect to the smooth tube.
- II. Over the range of Reynolds number, the heat transfer rate was also increased markedly for insert having 25 mm spacing in U-shapes. It increases 4 times better compared with the smooth tube.
- III. Heat transfer coefficient was increased by 1.2, 1.18, 1.06 times improved for three different spacings in U-shape inserts of 25 mm, 40 mm, 80 mm than the smooth tube. And the former insert was obviously better than the others.
- IV. Overall heat transfer enhancement efficiency was effectively increased for the three inserts likened with the smooth tube. Efficiency was increased 1.57 to 1.67, 1.32 to 1.40, 1.17 to 1.27 times respectively for 25 mm, 40 mm, 80 mm spacings in U-shape inserts. It is undoubtedly mark that, Ushape twisted insert of 25 mm spacings in Ushapes was the best among the others in the current experiment.

#### 6. ACKNOWLEDGEMENT

I am very grateful to almighty who have given me the chance to do the project and have given me patience and power to complete the project successfully. I wish to express my gratitude to my parents foremost. I am also grateful and indebted to the Heat Engine Laboratory members of Chittagong University of Engineering and Technology, without whom the task was impossible. Finally I would like to thank all of my teachers and staffs of Mechanical engineering department, Chittagong University of Engineering and Technology and also to my friends, who helped me directly or indirectly whenever it required.

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| 8. NOMENCLATURE |                               |                   |  |
|-----------------|-------------------------------|-------------------|--|
| Symbol          | Meaning                       | Unit              |  |
| W               | Twisted tape width            | (mm)              |  |
| W               | U- cut width                  | (mm)              |  |
| $d_e$           | U-shape depth                 | (mm)              |  |
| d               | Tube diameter                 | (m)               |  |
| r               | Radius                        | (m)               |  |
| L               | Tube length                   | (m)               |  |
| $L_{tap}$       | Twisted tape length           | (m)               |  |
| Α               | Area                          | (m <sup>2</sup> ) |  |
| $u_m$           | Mean velocity                 | (m/s)             |  |
| V               | Velocity                      | (m/s)             |  |
| т               | Mass flow rate                | (kg/s)            |  |
| ρ               | Density                       | $(kg/m^3)$        |  |
| μ               | Dynamic viscosity             | (kg/m-s)          |  |
| $C_p$           | Specific heat                 | (J/kg.K)          |  |
| Q               | Heat transfer rate            | (W)               |  |
| q               | Heat flax                     | $(W/m^2)$         |  |
| h               | Heat transfer coefficient     | $(W/m^2.K)$       |  |
| $k_w$           | Thermal conductivity          | (W/m.K)           |  |
| $T_o$           | Hot water temperature         | (°C)              |  |
| $T_i$           | Cold water temperature        | (°C)              |  |
| $T_{I}$         | Temperature of thermocouple 1 | (°C)              |  |
| $T_2$           | Temperature of thermocouple 2 | (°C)              |  |
| $T_3$           | Temperature of thermocouple 3 | (°C)              |  |
| $T_4$           | Temperature of thermocouple 4 | (°C)              |  |
| $T_5$           | Temperature of thermocouple 5 | (°C)              |  |
| $T_b$           | Bulk temperature              | (°C)              |  |
| $T_{wo}$        | Outer surface temperature     | (°C)              |  |
| $T_{wi}$        | Inner surface temperature     | (°C)              |  |
| у               | Twist ratio                   | Dimensionless     |  |
| Nu              | Nusselt number                | Dimensionless     |  |
| $\Delta P$      | Pressure drop                 | Dimensionless     |  |
| f               | Friction factor               | Dimensionless     |  |
| Pr              | Prandtl number                | Dimensionless     |  |
| Re              | Reynolds number               | Dimensionless     |  |
| η               | Thermal enhancement factor    | Dimensionless     |  |